The University Interscholastic League Number Sense Test • HS SAC • 2023

Read directions carefully before beginning test	DO NOT UNFOLD THIS SHEET UNTIL TOLD TO BEGIN		Score	Initials
		1st		
Contestant's Number		2nd		
		Final		

Directions: Do not turn this page until the person conducting this test gives the signal to begin. This is a ten-minute test. There are 80 problems. Solve accurately and quickly as many as you can in the order in which they appear. ALL PROBLEMS ARE TO BE SOLVED MENTALLY. Make no calculations with paper and pencil. Write only the answer in the space provided at the end of each problem. Problems marked with a (*) require approximate integral answers; any answer to a starred problem that is within five percent of the exact answer will be scored correct; all other problems require exact answers.

The person conducting this contest should explain these directions to the contestants.

STOP -- WAIT FOR SIGNAL!

(1) 2023 + 3202 =	(18) $6\frac{1}{4} \times 16 =$
(2) $2023 - 4 \times 2023 =$	(19) $6\frac{3}{4} \times 16 =$
(3) $\frac{1}{8} \div 4.5 =$	*(20) 804 × 649 =
(4) $37\frac{1}{2}\% =$ (proper fraction)	(21) 27 × 23 =
(5) $(1+2) \div 3 - 4 \times 5 =$	(22) 144 ÷ 0.08333 =
(6) $23^2 =$	(23) Write twelve and three-eighths million in digits.
(7) $111 \times \frac{1}{37} = $	(24) [9+23 × 21+11] ÷ 5 has a remainder of
(8) MMXXIII = (Arabic Numeral)	(25) $12\frac{1}{4} \times 8\frac{1}{4} =$ (mixed number)
(9) 2023 ÷ 3 has a remainder of	(26) $\$4.60 + \$7.29 - \$9.88 = \$$
*(10) 3202 + 2023 - 322 =	(27) $\$4.45 + \$7.27 - \$9.88 = \$$
(11) If a half dozen eggs cost \$2.40, then 9 eggs should cost \$	(28) $$4.60 + $7.29 - $9.68 = $$
(12) The LCM of 12 and 14 is	(29) 239 base 10 is written as base 4
(13) 312 × 14 is	*(30) $\sqrt{992023} =$
(14) $18 \times \frac{18}{19} =$ (mixed number)	(31) 2399 × 1 + 1 =
(15) $24^2 - 26^2 = 4 \times$	(32) $3600 = [4(12 + B)]^2$. Find B, B > 0
(16) The largest prime less than 29 is	(33) If $f(x) = x^2 - 6x + 9$, then $f(-20) =$
(17) $6\frac{1}{2} \times 16 =$	(34) Given: 2, 3, 5, 7, 11, m, 17, n, Find m + n

- (35) The sum of three consecutive odd integers is 135. The larger of the integers is _____
- $(36) \ 4\frac{3}{5} \times 5\frac{3}{4} = _$
- (37) How many integers between 9 and 63 are divisible by 7? _____
- (38) {m,a,r,c,h} ∪ [{a,p,r,i,l} ∩ {m,a,y}] contains how many elements? _____
- (39) Let $\frac{x-5}{x+6} + \frac{x+6}{x-5} = 2\frac{B}{C}$. Find B.
- *(40) $\sqrt[3]{9232111} =$ _____
- (41) $(3^3 + 7^3) \div 10$ has a remainder of _____
- $(42) \ 23_7 \times 5_7 + 236_7 = \underline{\qquad} 7$
- (43) The coefficient of the x^3y^2 term of $(x + y)^5$ is _____
- (44) The arithmetic mean of 9, 22, and 23 is _____
- (45) If x + y = 11 and 2x y = 13, then y =_____
- $(46) \ (304)^2 = _$
- (47) Let $4\frac{2}{m} \times n\frac{21}{22} = 13$, where m, n are natural numbers. Find m + n.
- (48) The sum of the roots of $6x^2 + 8x 7 = 0$ is _____
- (49) $(8^3 2^3) \div (8 2) =$ _____
- *(50) 992023 ÷ 923 = _____
- (51) The 11th term of 1, 2, 5, 10, 17, 26, ... is 101. The 10th term is _____
- (52) 0.25 is what per cent less than 2.5? ____%
- $(53) \ \frac{1}{3} + \frac{1}{6} + \frac{1}{10} + \frac{1}{15} = \underline{\qquad}$
- (54) (4+5+9+14+23+37+60+97)+ (157+254+411) =_____
- (55) If $\sqrt{16 \sqrt{12\sqrt{4 x}}} = 2$, then x =_____
- (56) Two dice are rolled. Find the probability that the sum of the numbers is greater than 10. _____

 $(57) \ 22^2 + 18^2 = _$

- (58) The perimeter of a square is increased from 18 cm to 22 cm. Find the corresponding increase in its area. _____ cm²
- (59) 2023₄ ÷ 3₄ has a remainder of _____
- *(60) If 134.64 pesos equals 8 dollars, then 22 dollars equals _____ pesos.
- (61) 5 fathoms = ______ feet
- (62) If $(\sqrt{a^6})(\sqrt[6]{a}) = (\sqrt[n]{a^k})$, where n and k are relatively prime, then k = ____
- (63) Let 2x y = 3 and x + y = 5. Find 2x + y.
- (64) The det $\begin{vmatrix} x & 2 \\ 3 & 4 \end{vmatrix} = det \begin{vmatrix} 2 & 3 \\ 5 & 7 \end{vmatrix}$ and x = ______
- (65) If f(x) = 2 x and g(x) = 2x 1, then g(f(3) =_____
- (66) Which of the following is not a pentagonal number, 12, 15, 35?
- (67) $20^6 \div 11$ has a remainder of _____
- (68) Change $\frac{8}{25}$ to a base 5 decimal. _____5
- (69) $(Sin(Arccos(-0.5)))^2 =$ _____
- *(70) $(1+2+3+...+9+10)^2 =$ _____
- (71) $f(x) = \frac{7-2x}{3+5x}$ and $f^{-1}(6) =$ _____
- (72) Let $g(x) = (2x + 1)^4$. Find g'(1).
- (73) Find x, $7 \le x \le 13$, if $2x + 1 \cong 23 \pmod{7}$.
- (74) $h(x) = x^3 2x$ has an inflection point at (a, b). a + b = _____
- (75) The axis of symmetry of $6x^2 + 8x = 7$ is x =_____
- (76) $\int_0^4 x \, dx =$ _____
- (77) The slope of the tangent line to $4 = x^2 + y^2$ at y = 2 is ______
- (78) Given: 2, 8, 18, 32, k, 72, 98,... . k = _____
- (79) 221 × 17 = _____
- *(80) 27 × 142857 = _____