

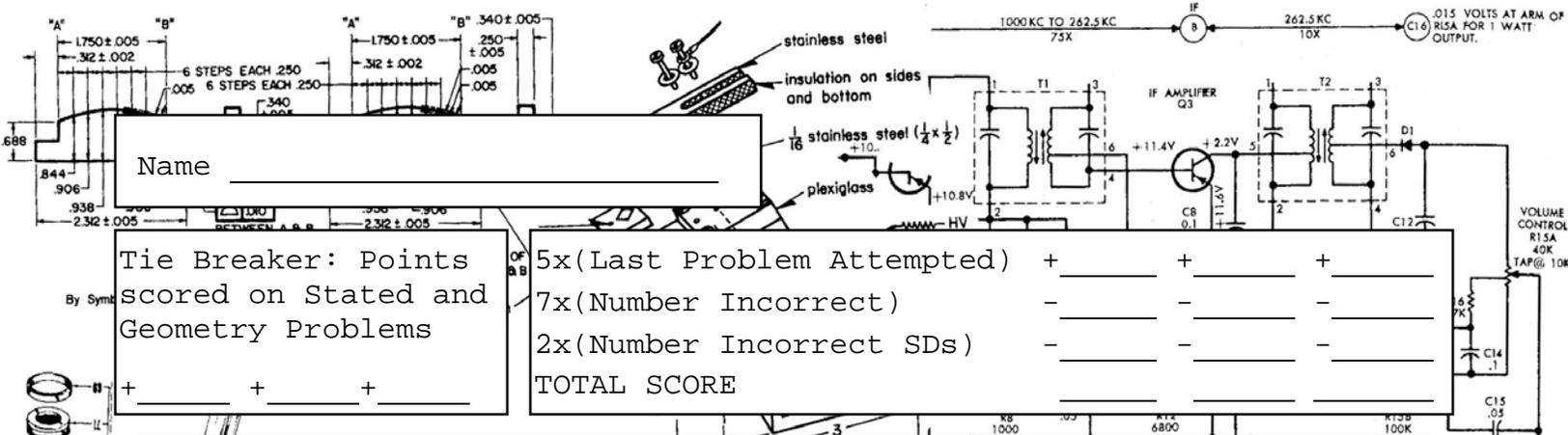


UNIVERSITY INTERSCHOLASTIC LEAGUE

Calculator Applications Study Packet 2020

This Calculator Applications packet contains tests and keys from **only** 2020 Invitational A, B and District. Region and State are not available.

This item is intended for High School grade levels.



Name _____

Tie Breaker: Points scored on Stated and Geometry Problems
 + _____ + _____ + _____

5x(Last Problem Attempted) + _____ + _____ + _____
 7x(Number Incorrect) - _____ - _____ - _____
 2x(Number Incorrect SDs) - _____ - _____ - _____
 TOTAL SCORE _____

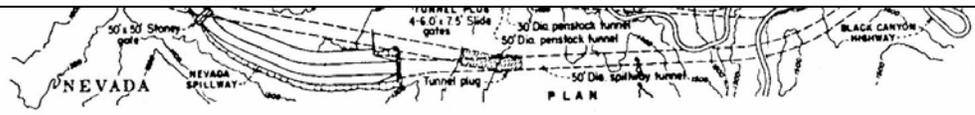
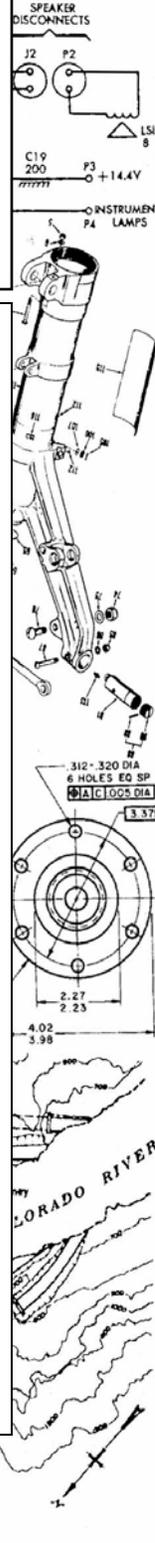
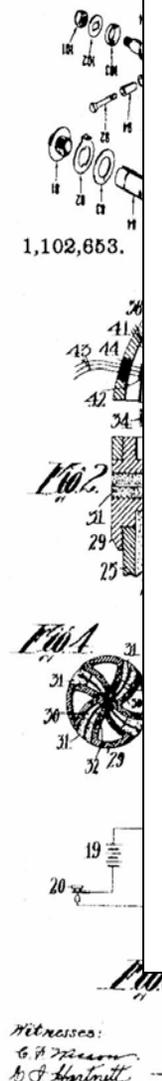
UIL Calculator Applications

Test 20A

(Invitational A)

DO NOT OPEN THE TEST UNTIL INSTRUCTED TO BEGIN

- I. Calculator Applications rules and scoring—See UIL Constitution
- II. How to write the answers
 - A. For all problems except stated problems as noted below—write three significant digits.
 - 1. Examples (* means correct but not recommended)
 Correct: 12.3, 123, 123.*, 1.23x10*, 1.23x10^{0*}, 1.23x10¹, 1.23x10⁰¹, .0190, 0.0190, 1.90x10⁻²
 Incorrect: 12.30, 123.0, 1.23(10)², 1.23•10², 1.230x10², 1.23*10², 0.19, 1.9x10⁻², 19.0x10⁻³, 1.90E-02, (0.190)
 - 2. Plus or minus one digit error in the third significant digit is permitted.
 - B. For stated problems
 - 1. Except for integer, dollar sign, and significant digit problems, as detailed below, answers to stated problems should be written with three significant digits.
 - 2. Integer problems are indicated by (integer) in the answer blank. Integer problems answers must be exact, no plus or minus one digit, no decimal point or scientific notation.
 - 3. Dollar sign (\$) problems should be answered to the exact cent, but plus or minus one cent error is permitted. Answers must be in fixed notation. The decimal point and cents are required for exact-dollar answers.
 - 4. Significant digit problems are indicated by underlined numbers and by (SD) in the answer blank. See the UIL Constitution and Contest Manual for details.
- III. Some symbols used on the test
 - A. Angle measure: rad means radians; deg means degrees.
 - B. Inverse trigonometric functions: arcsin for inverse sine, etc.
 - C. Special numbers: π for 3.14159 ...; e for 2.71828 ...
 - D. Logarithms: Log means common (base 10); Ln means natural (base e); exp(u) means e^u.



20A-1. $(3.54 + 5.73) \times 0.996$ ----- 1= _____

20A-2. $(0.259 + 0.278) \times (-0.39) - 0.443$ ----- 2= _____

20A-3. $(3.29 + 12.8 - 2.45)/(\pi) + 0.648$ ----- 3= _____

20A-4. $\frac{(53.8)(28.9 - 13.9 + 25.6)}{(-84)(10.8)}$ ----- 4= _____

20A-5. $\frac{(-0.00711 - 0.00567)(5.66)}{\{(-8.21)/(-68.7)\}} - (\pi - 1.2)$ ----- 5= _____

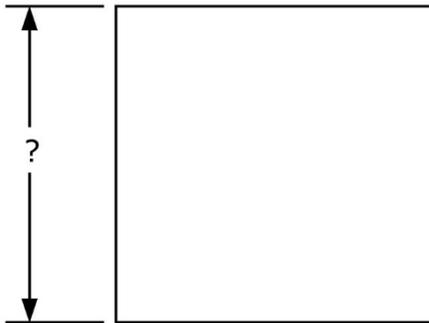
20A-6. What is the cube root of -957 ? ----- 6= _____

20A-7. What is the remainder of 4830 divided by 5.36? ----- 7= _____

20A-8. What is 2 cubed divided by 3 squared? ----- 8= _____

20A-9.

SQUARE

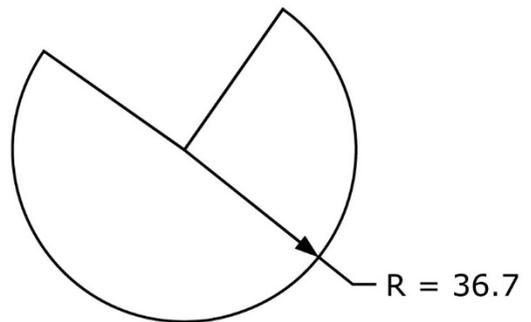


Area = 0.245

20A-9 = _____

20A-10.

THREE QUARTER CIRCLE



Area = ?

20A-10 = _____

20A-11. $\frac{(-0.0817)(0.0178) + (0.0651)(-0.044)}{-3.57 + 0.496 - (-5.54)(0.35)}$ ----- 11= _____

20A-12. $\frac{-0.0701 + 0.0445}{(0.711)(1.54)(-5.61 \times 10^{-9})} + (757 + 1250)(592 - 105)$ ----- 12= _____

20A-13. $\frac{2.33 \times 10^5 + 3.32 \times 10^5}{(-0.913)(-0.632) + 0.894} + \frac{5120 - 3310 + 7320}{(-3.76 \times 10^{-5})(-390)}$ ----- 13= _____

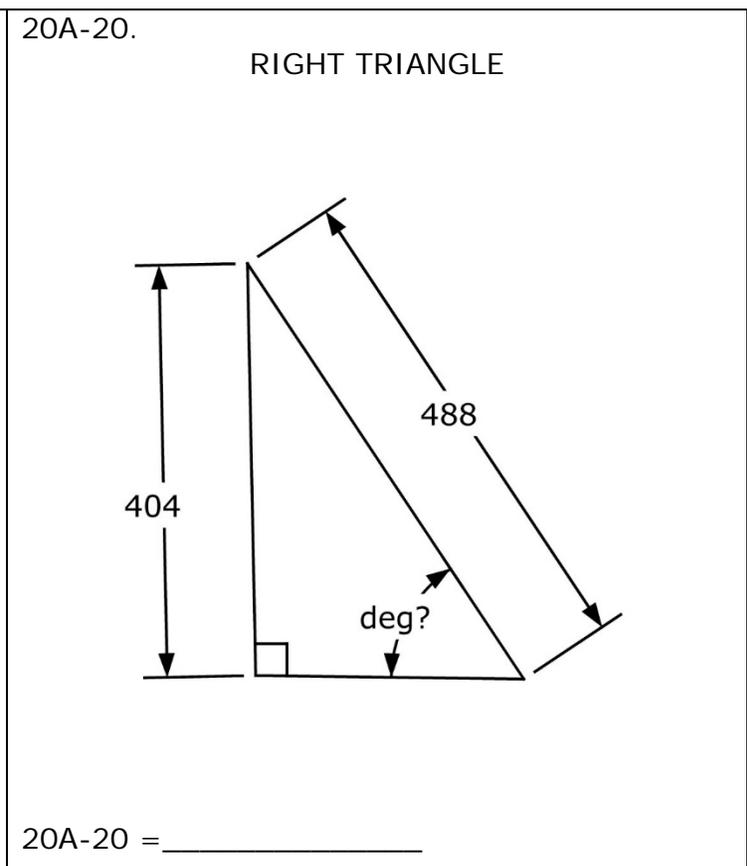
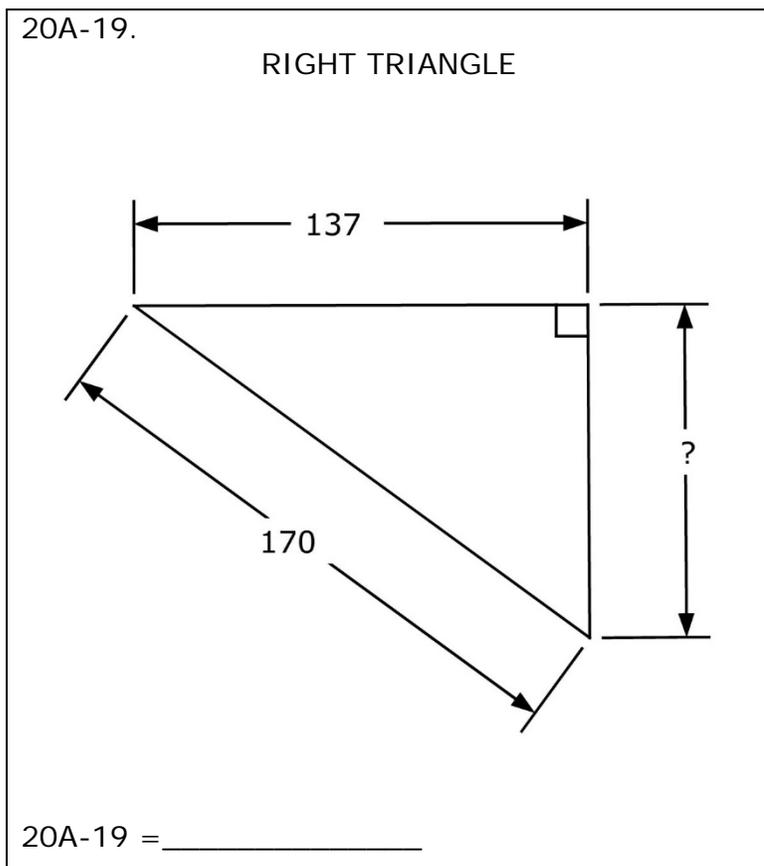
20A-14. $\frac{367 + 300 - 339}{(0.247)(5.16)} - \frac{(95300)(2.68 \times 10^{-4} + 1.03 \times 10^{-4})}{0.649 + 0.462 - 0.84}$ ----- 14= _____

20A-15. $\frac{1.33 \times 10^5 + 3.87 \times 10^5 - (97300 + 1.18 \times 10^5)(\pi - 1.95)}{(-555)(-7.84)(-7.65)(514 - 253 + 1520)}$ ----- 15= _____

20A-16. A ream of paper has 500 sheets. A box has 10 reams, and a pallet has 40 boxes. How many sheets of paper are in a pallet? ----- 16= _____ integer

20A-17. US lifespan is 78.7 yr. The average human heartbeat rate is 72 beats/min. How many times does the heart beat in a lifetime? ----- 17= _____

20A-18. Wally has \$3500 for a "new" car. He finds a car for \$9000, and he can take out a 3-yr loan at 0% annual interest for the difference, making equal monthly payments. If insurance and gas are \$182 monthly, what does he pay monthly? ----- 18= \$ _____



20A-21. $\frac{1}{\pi + 2.48} + \frac{1}{3.07 - 4.15} + \frac{1}{(0.805)}$ ----- 21=_____

20A-22. $\sqrt{\frac{(4.66)(\pi)}{166 + 29.8}} + 0.264$ ----- 22=_____

20A-23. $(-8.82)(-0.0993)\sqrt{(-0.942)^2/0.758} + 1/\sqrt{0.306 + 2.17}$ ----- 23=_____

20A-24. $\left[\frac{\pi + 1.3 + \sqrt{0.492/0.165}}{-54.6 + 30.5}\right]^2$ ----- 24=_____

20A-25. $(1.52)(5.27) + \sqrt{(38.5)/(3.79)} + [(0.262)(8.24)]^2$ ----- 25=_____

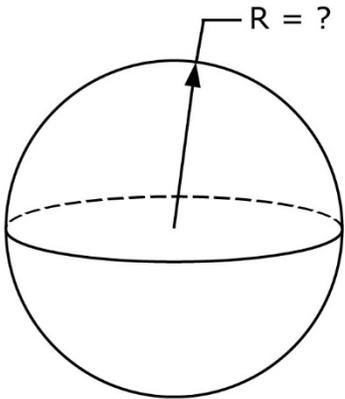
20A-26. A contact lens is, on a mass basis, considerably more expensive than gold. Six lenses cost \$25, and each lens weighs 14 mg. Gold costs \$18,000/lb. What is the ratio of the cost/mass of a lens to the cost/mass of gold? ----- 26=_____

20A-27. Greenland has the lowest population density of all countries. It has a land area of 836,297 mi² with a population of 55,877 people. What is the percent error in its reported population density of 0.08 people/mi²? ---- 27=_____%(SD)

20A-28. Mannie has \$5000 but needs \$5800 in two years. What annual interest rate must she find? ----- 28=_____%

20A-29.

SPHERE

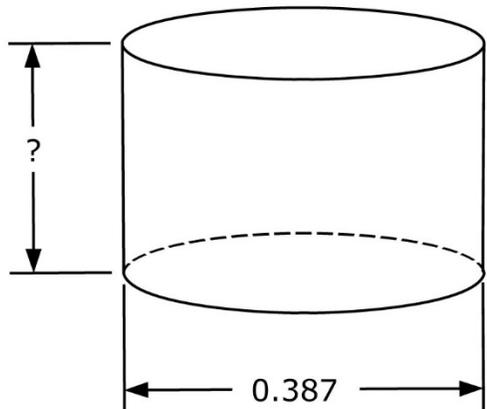


Surface Area = 623

20A-29 = _____

20A-30.

CYLINDER



Volume = 0.0291

20A-30 = _____

20A-31. $\sqrt{\frac{6.27}{\sqrt{91 + 65.4}}} \times \left[\frac{1}{(8.18 - 7.95)^2} + \frac{1}{(0.738 + 0.729)^2} \right]$ ----- 31 = _____

20A-32. $\left[\frac{-9.43 \times 10^{-6}}{3.97 \times 10^{-4} + 2.03 \times 10^{-4}} + 0.0174 \right] \times \left\{ 759 + (-39)^2 - \sqrt{4.10 \times 10^6} \right\}$ 32 = _____

20A-33. $\frac{[0.0222/(0.508 + 0.484) + 1/(7.04)]^{1/2}}{(5.2 + 39.7)^2 \times \sqrt{0.752 - (-0.229)}}$ ----- 33 = _____

20A-34. $\frac{\sqrt{(80800)/\{(12400)/\sqrt{19300}\}}}{5.39 + (0.889)(\pi)} + \{8.48 + 12.1\}^{1/2}$ ----- 34 = _____

20A-35. $\frac{\left[\frac{(716 + 587)}{(996 + 3730)} \right]^2 + \sqrt{\frac{0.00139 + 0.00251}{\sqrt{0.559}}}}{\{(658)/(-906)\}^2}$ ----- 35 = _____

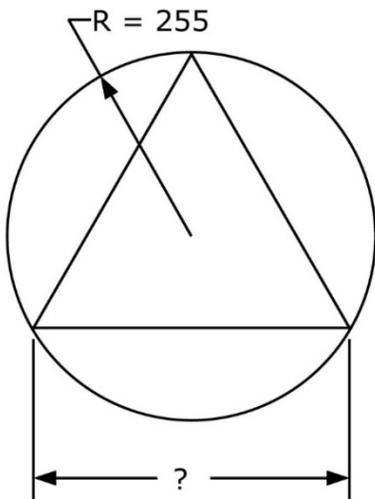
20A-36. It's estimated that there are as many as 10^{19} insects in the world.

What is the average insect density on earth's surface? ----- 36 = _____ insects/ft²

20A-37. John and Jose start running together on a 440-yd track. Jose runs a mile in 5.8 min, 10% faster than John. How long will it take Jose to lap John? ----- 37 = _____ min

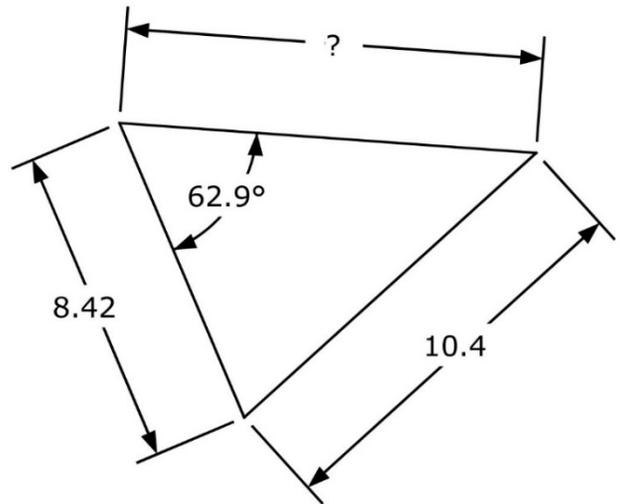
20A-38. Translucent plates absorb light according to $I = I_0 \exp(-\alpha t)$, where I is the transmitted light, I_0 the incident light, t the thickness of the plate and α is an absorption constant. What thickness of plate is needed to absorb 85% of the incident light if α equals 0.16/mm? ----- 38 = _____ mm

20A-39. CIRCLE AND EQUILATERAL TRIANGLE



20A-39 = _____

20A-40. SCALENE TRIANGLE



20A-40 = _____

20A-41. $\frac{10^{-(2.74 - 6.56)}}{3.07 \times 10^6 + 1.00 \times 10^6}$ ----- 41 = _____

20A-42. $-5.47 e^{0.207} + (-1.13) e^{-0.499}$ ----- 42 = _____

20A-43. $\frac{4.74 - 5.54}{\text{Log}(9.98 + 7.35)}$ ----- 43 = _____

20A-44. $(877 + 1430)^{1/3} + 1/\{(604)^{-0.371}\}$ ----- 44 = _____

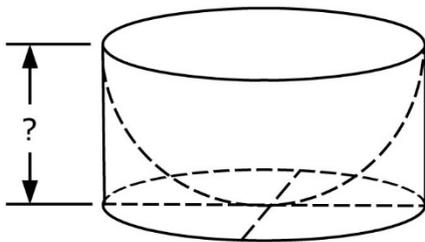
20A-45. $(\text{deg}) \sin \left[90^\circ \times \frac{(-83000)}{(1.57 \times 10^5)} \right] + \cos \{ 33.6^\circ - 31.2^\circ \}$ ----- 45 = _____

20A-46. If it takes 22 blows to fill an 8 in diameter balloon, what is the diameter of a balloon that requires 85 blows to fill? ----- 46 = _____ in

20A-47. Earth's gravitational constant is latitude dependent. At the equator (0°), it is 32.0878 ft/s^2 . At the north pole (90°), it is 32.2577 ft/s^2 . Other values are (25° , 32.1180), (50° , 32.1873) and (60° , 32.2151). At what latitude is the gravitational constant equal to the "official" UIL value, 32.174 ft/s^2 ? ----- 47 = _____ $^\circ$

20A-48. (rad) For what value of x between 0 and $\pi/2$ does $\tan x = 1-x$? ----- 48 = _____

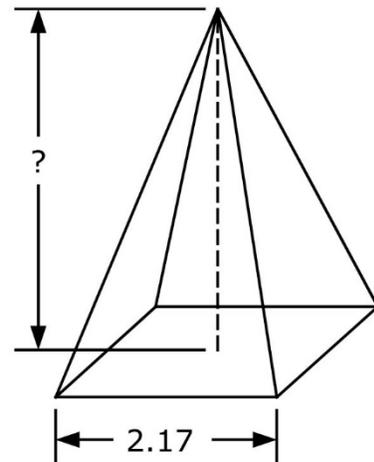
20A-49. CYLINDER WITH HEMISPHERICAL CAVITY



Volume = 464

20A-49 = _____

20A-50. SQUARE PYRAMID



Total Surface Area = 19.6

20A-50 = _____

20A-61. The density of a spherical particle is 2.54 g/cc. What is the particle diameter if the surface area per unit mass is 20 m²/g? ----- 61= _____ μm

20A-62. What is 6.022 × 10²³ (Avogadro's number) raised to the 50th power? ----- 62= _____

20A-63. Randy fires a gun with a muzzle velocity of 1000 ft/s. The bullet travels 3 mi, and the initial trajectory angle is less than 45°. Neglecting air resistance, what was the bullet maximum vertical height? ----- 63= _____ ft

20A-64.
CONGRUENT ISOSCELES TRIANGLES

20A-64 = _____

20A-65.
CIRCLES

20A-65 = _____

20A-66.
$$\frac{\sqrt{(3.96)^3} \times \{e^{(7.31)(0.0589)}\}^3}{\sqrt[3]{e^{(2.14)} \times e^{(-0.83)}}}$$
 ----- 66= _____

20A-67. $(92.8 - 22.6)^2 + (1.12 + 3.99)e^{\ln(446)}$ ----- 67= _____

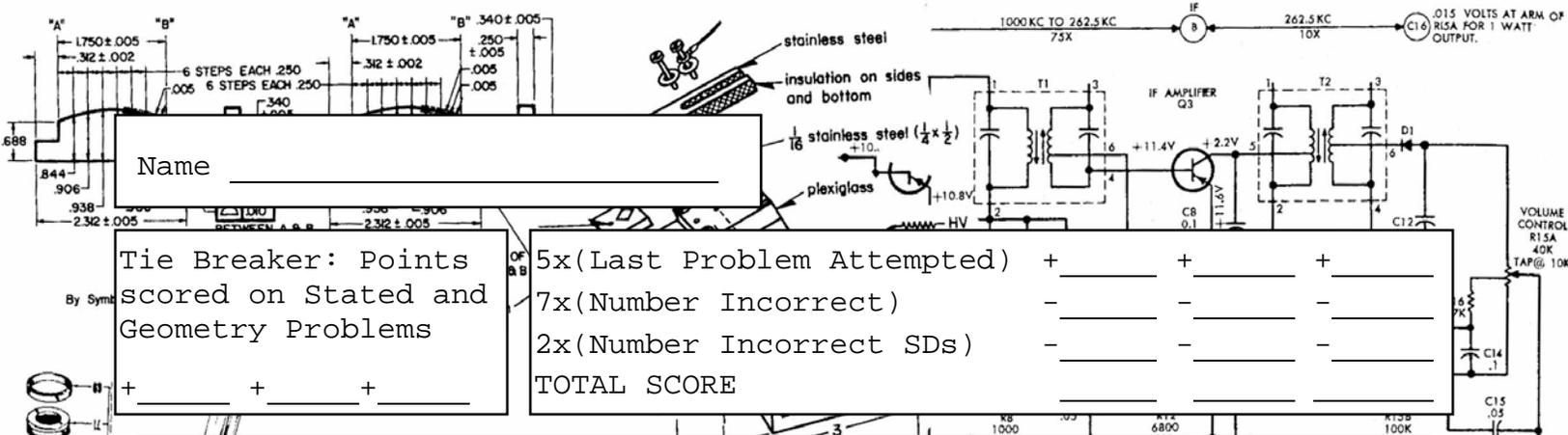
20A-68. $(\text{rad}) \frac{98.2}{6(7.95)} \{ (2.88) + (1.93)\sin(\pi) \}^5$ ----- 68= _____

20A-69. $1 + 0.73 + (0.73)^2 + \frac{(0.73)^4}{8} - \frac{(0.73)^5}{15}$ ----- 69= _____

20A-70. $\frac{(50.8)}{(-0.963)} - \frac{(0.571)}{(-0.142)^2} \ln \left[\frac{(-0.0972)^2 + (0.00468)}{(-0.527) + \sqrt{1.4}} \right]$ ----- 70= _____

20A-1	= 9.23 = 9.23×10^0	20A-11	= 0.00380 = 3.80×10^{-3}	20A-21	= 0.494 = 4.94×10^{-1}
20A-2	= -0.652 = -6.52×10^{-1}	20A-12	= 5.15×10^6	20A-22	= 0.537 = 5.37×10^{-1}
20A-3	= 4.99 = 4.99×10^0	20A-13	= 1.01×10^6	20A-23	= 1.58 = 1.58×10^0
20A-4	= -2.41 = -2.41×10^0	20A-14	= 127 = 1.27×10^2	20A-24	= 0.0655 = 6.55×10^{-2}
20A-5	= -2.55 = -2.55×10^0	20A-15	= -0.00444 = -4.44×10^{-3}	20A-25	= 15.9 = 1.59×10^1
20A-6	= -0.985 = -9.85×10^{-1}	20A-16	= 200,000 integer	20A-26	= 7.50 = 7.50×10^0
20A-7	= 0.640 = 6.40×10^{-1}	20A-17	= 2.98×10^9	20A-27	= 19.73 = 1.973×10^1 (4SD)
20A-8	= 0.889 = 8.89×10^{-1}	20A-18	= \$334.78	20A-28	= 7.70 = 7.70×10^0
20A-9	= 0.495 = 4.95×10^{-1}	20A-19	= 101 = 1.01×10^2	20A-29	= 7.04 = 7.04×10^0
20A-10	= 3170 = 3.17×10^3	20A-20	= 55.9 = 5.59×10^1	20A-30	= 0.247 = 2.47×10^{-1}

20A-31	= 13.7 = 1.37×10^1	20A-41	= 0.00162 = 1.62×10^{-3}	20A-51	= 11.9 = 1.19×10^1	20A-61	= 0.118 = 1.18×10^{-1}
20A-32	= 0.430 = 4.30×10^{-1}	20A-42	= -7.41 = -7.41×10^0	20A-52	= 4.60×10^6	20A-62	= 9.71×10^{1188}
20A-33	= 0.000203 = 2.03×10^{-4}	20A-43	= -0.646 = -6.46×10^{-1}	20A-53	= -0.00858 = -8.58×10^{-3}	20A-63	= 1080 = 1.08×10^3
20A-34	= 8.21 = 8.21×10^0	20A-44	= 24.0 = 2.40×10^1	20A-54	= 1.19 = 1.19×10^0	20A-64	= 205 = 2.05×10^2
20A-35	= 0.281 = 2.81×10^{-1}	20A-45	= 0.261 = 2.61×10^{-1}	20A-55	= 0.000104 = 1.04×10^{-4}	20A-65	= 11.4 = 1.14×10^1
20A-36	= 1820 = 1.82×10^3	20A-46	= 12.6 = 1.26×10^1	20A-56	= 12.7 = 1.27×10^1	20A-66	= 18.5 = 1.85×10^1
20A-37	= 16.0 = 1.60×10^1	20A-47	= 45.4 = 4.54×10^1	20A-57	= 12.0 = 1.20×10^1	20A-67	= 7210 = 7.21×10^3
20A-38	= 11.9 = 1.19×10^1	20A-48	= 0.480 = 4.80×10^{-1}	20A-58	= 616.00 = 6.16×10^2	20A-68	= 408 = 4.08×10^2
20A-39	= 442 = 4.42×10^2	20A-49	= 7.62 = 7.62×10^0	20A-59	= 12.6 = 1.26×10^1	20A-69	= 2.28 = 2.28×10^0
20A-40	= 11.0 = 1.10×10^1	20A-50	= 3.26 = 3.26×10^0	20A-60	= 265 = 2.65×10^2	20A-70	= 55.9 = 5.59×10^1



Name _____

Tie Breaker: Points scored on Stated and Geometry Problems
 + _____ + _____ + _____

5x(Last Problem Attempted) + _____ + _____ + _____
 7x(Number Incorrect) - _____ - _____ - _____
 2x(Number Incorrect SDs) - _____ - _____ - _____
 TOTAL SCORE _____

UIL Calculator Applications

Test 20B

(Invitational B)

DO NOT OPEN THE TEST UNTIL INSTRUCTED TO BEGIN

- I. Calculator Applications rules and scoring—See UIL Constitution
- II. How to write the answers

A. For all problems except stated problems as noted below—write three significant digits.

1. Examples (* means correct but not recommended)

Correct: 12.3, 123, 123.*, 1.23x10*, 1.23x10^{0*}
 1.23x10¹, 1.23x10⁰¹, .0190, 0.0190, 1.90x10⁻²

Incorrect: 12.30, 123.0, 1.23(10)², 1.23•10², 1.230x10²,
 1.23*10², 0.19, 1.9x10⁻², 19.0x10⁻³, 1.90E-02

2. Plus or minus one digit error in the third significant digit is permitted.

B. For stated problems

1. Except for integer, dollar sign, and significant digit problems, as detailed below, answers to stated problems should be written with three significant digits.

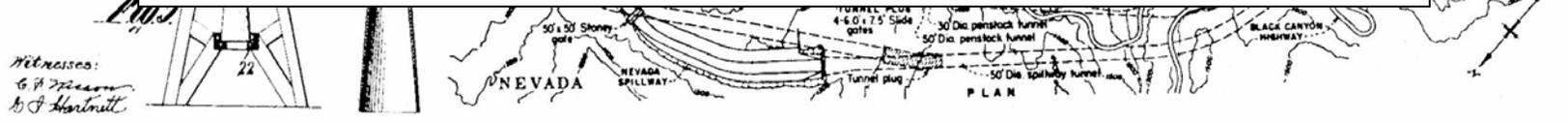
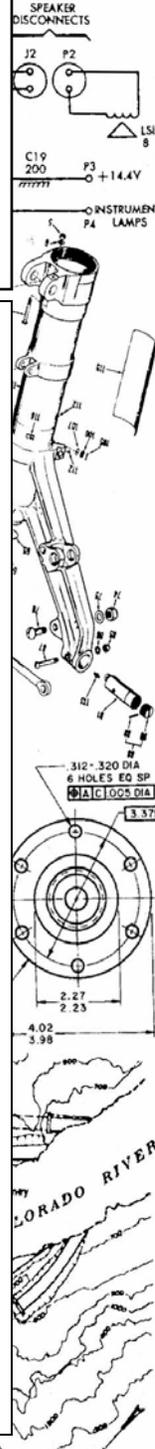
2. Integer problems are indicated by (integer) in the answer blank. Integer problems answers must be exact, no plus or minus one digit, no decimal point or scientific notation.

3. Dollar sign (\$) problems should be answered to the exact cent, but plus or minus one cent error is permitted. Answers must be in fixed notation. The decimal point and cents are required for exact-dollar answers.

4. Significant digit problems are indicated by underlined numbers and by (SD) in the answer blank. See the UIL Constitution and Contest Manual for details.

III. Some symbols used on the test

- A. Angle measure: rad means radians; deg means degrees.
- B. Inverse trigonometric functions: arcsin for inverse sine, etc.
- C. Special numbers: π for 3.14159 ...; e for 2.71828 ...
- D. Logarithms: Log means common (base 10); Ln means natural (base e); exp(u) means e^u.



20B-1. $(0.101/0.0985) + 0.128$ ----- 1= _____

20B-2. $(-8.97 + 4.55 - 1.12) \times \pi$ ----- 2= _____

20B-3. $\frac{(-0.162)(0.688)(0.234)}{0.167} + 0.0778$ ----- 3= _____

20B-4. $\frac{(-0.671)(0.794 - 0.659 + 2.78)}{(0.313)(-0.036)}$ ----- 4= _____

20B-5. $\frac{(-0.00593 - 0.0047)(0.195)}{\{(-0.409)/(0.637)\}} - (0.00353 - 5.56 \times 10^{-4})$ ----- 5= _____

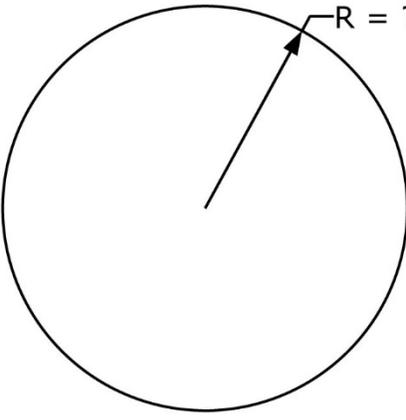
20B-6. What is the positive difference of 37.5 and 10π ? ----- 6= _____

20B-7. What number when divided by 405 yields 77.8? ----- 7= _____

20B-8. Solve for x if $4x = 17/x^2$. ----- 8= _____

20B-9.

CIRCLE

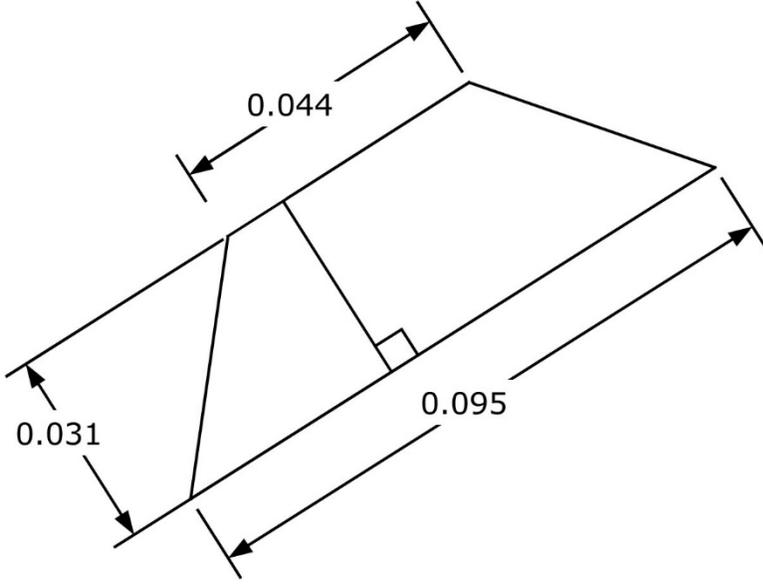


Perimeter = 894

20B-9 = _____

20B-10.

ISOSCELES TRAPEZOID



Area = ?

20B-10 = _____

20B-11. $\frac{(6340 + 6120)}{(0.24 - 0.259)} + \frac{(-2.65 \times 10^6 + 3.98 \times 10^6)}{(8.7 - 1.12)}$ ----- 11 = _____

20B-12. $\frac{-237(3.48 \times 10^{-5} + 1.31 \times 10^{-5})}{(289 - 533)(792)} - \frac{-7.61 \times 10^{-9}}{-0.345 - 0.275}$ ----- 12 = _____

20B-13. $\frac{8.49 \times 10^5 + 3.22 \times 10^6}{(-1.58)(-0.513) + 0.852} + \frac{5620 - 4750 + 26500}{(0.0294)(0.0491)}$ ----- 13 = _____

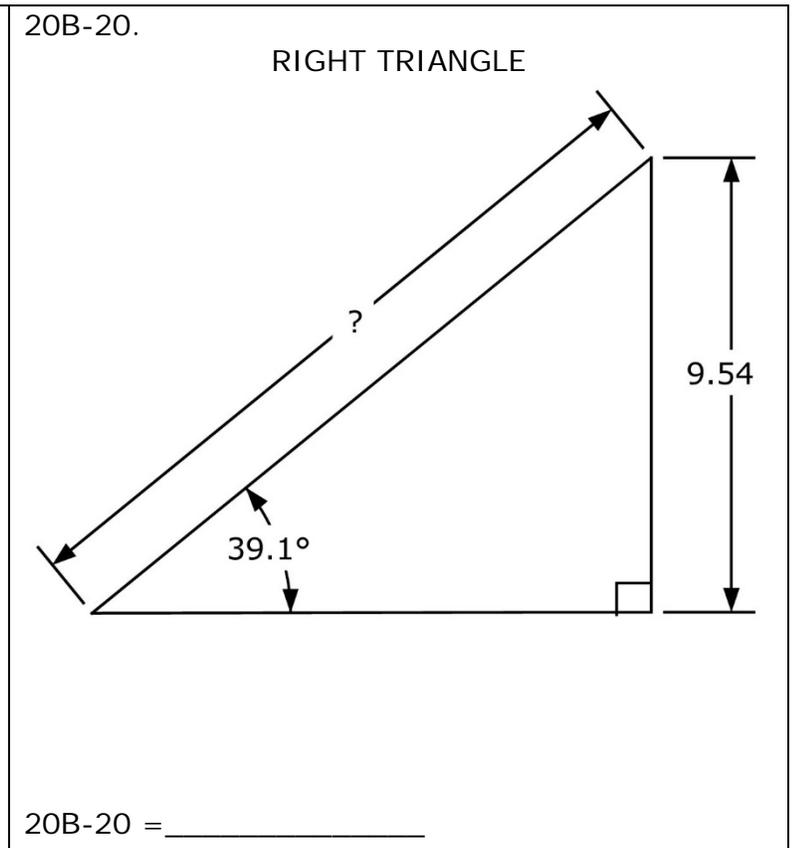
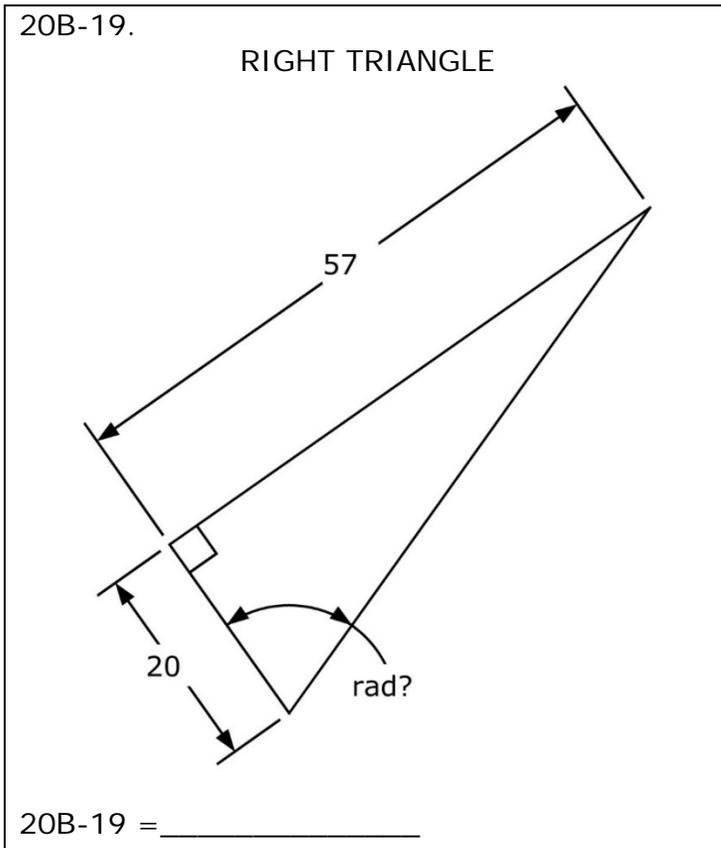
20B-14. $\frac{(4690 + 3320 - 2250)(0.00761 + 0.036 - 0.0199)}{(5.78 - 3.18)(-7.32)(-7.74 - 6.24)}$ ----- 14 = _____

20B-15. $\frac{(82100 + 29700 - 44900)(0.749 - 0.171 - 0.596)}{(-55.8)(-6.14)(-21.9)(8.45 + 7.8 + 36.4)}$ ----- 15 = _____

20B-16. In 2019, the US national debt reached 22 trillion dollars. If the population of the US in 2019 was 327.2 million people, what is the average per capita debt? ----- 16 = \$ _____

20B-17. What is the percent error in assuming the value 3 for π ? ----- 17 = _____ %

20B-18. If a person with 20-20 vision can read letters that are 0.2 in tall when standing 20 ft away, how tall should letters be if the person can read them from a distance of 1 mi? ----- 18 = _____ ft



20B-21. $\frac{-0.124 + 1/(-6.84)}{1/(0.457) + 2.8} + \frac{1}{(-5.21)}$ ----- 21= _____

20B-22. $\sqrt{\frac{(7.64)(7.19)}{339 + 142}} + 0.0902$ ----- 22= _____

20B-23. $[-24.3 + \sqrt{201}]^2 \times [392 + 863]^2 \times \sqrt{2.45/5.63}$ ----- 23= _____

20B-24. $\left[\frac{2.47 + 1.24 + \sqrt{0.487/0.781}}{-4.89 + 2.98} \right]^2$ ----- 24= _____

20B-25. $(0.866)(0.862)\sqrt{(-0.171)^2/0.585} + 1/\sqrt{33.8 + 43.3}$ ----- 25= _____

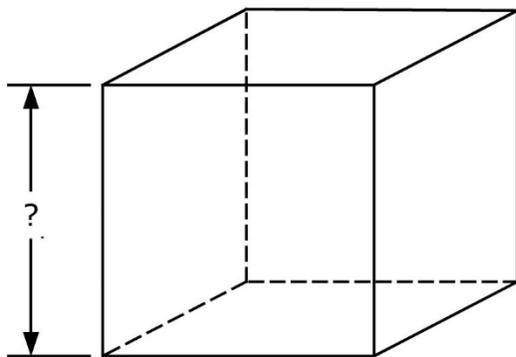
20B-26. The Singapore Flyer is the second-largest Ferris wheel in the world, 165 meters in diameter. If it takes 30 min to go around once, what is the car velocity? ----- 26= _____ m/s

20B-27. William lives 2.75 mi from high school. He can either walk to school or rent a scooter. Scooters cost \$1 to unlock and \$0.15 for each mile or fraction of a mile. If he wants to spend no more than \$10/wk on transportation, how many times weekly can he take a scooter round-trip to/from school? ----- 27= _____ integer

20B-28. Andy uses a 25-ft tape measure to measure a canoe. He measures 16 ft 4.53 in. Later he finds that his tape measure is not accurate. The tape measure total length is actually only 24 ft 11.48 in. What is the actual canoe length? ----- 28= _____ ft(SD)

20B-29.

CUBE

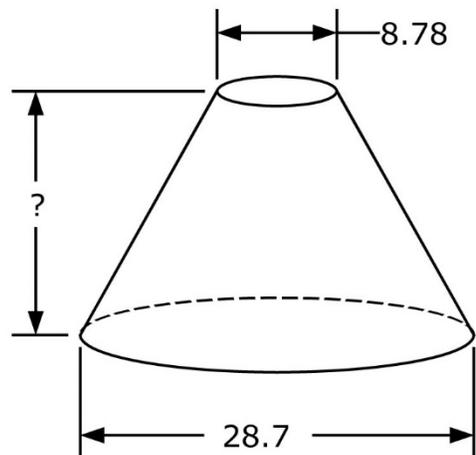


Surface Area = 0.773

20B-29 = _____

20B-30.

FRUSTUM



Volume = 5340

20B-30 = _____

20B-41. $10^{-\{(0.153 - 0.812)/(0.706 + 0.52)\}}$ ----- 41 = _____

20B-42. $\frac{(4.70 \times 10^{-5})}{(-4.67 \times 10^{-5})} [1 - e^{-(0.885)(0.698)}]$ ----- 42 = _____

20B-43. $(-0.475) \text{Log} \{ (0.464)(\pi + 1/0.313) \}$ ----- 43 = _____

20B-44. $(36900 + 41400)^{-(0.71 + 0.418)}$ ----- 44 = _____

20B-45. (deg) $\frac{\cos\{(37^\circ)/(1.83)\}}{\sin\{116^\circ - 200^\circ\}}$ ----- 45 = _____

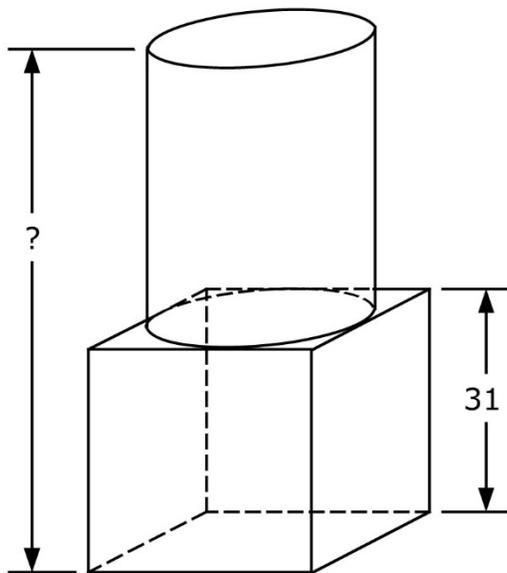
20B-46. A 6-in long bag holds 108 candies. How many candies are in a 16-in long bag of identical shape? ----- 46 = _____

20B-47. Wire diameter is inversely proportional to $\exp(\text{gage number}/10)$. Some (gage number, wire diameter) pairs are: (0, 0.34 in), (10, 0.134 in), (20, 0.035 in), (30, 0.012 in). What is the percent error in the interpolated value for a 25 gage wire if the actual diameter is 0.020 in? ----- 47 = _____ %

20B-48. (rad) Solve for the smallest positive value of x if $x \sin(x) = \cos(x) + x - 8$. ----- 48 = _____

20B-49.

CUBE AND CYLINDER

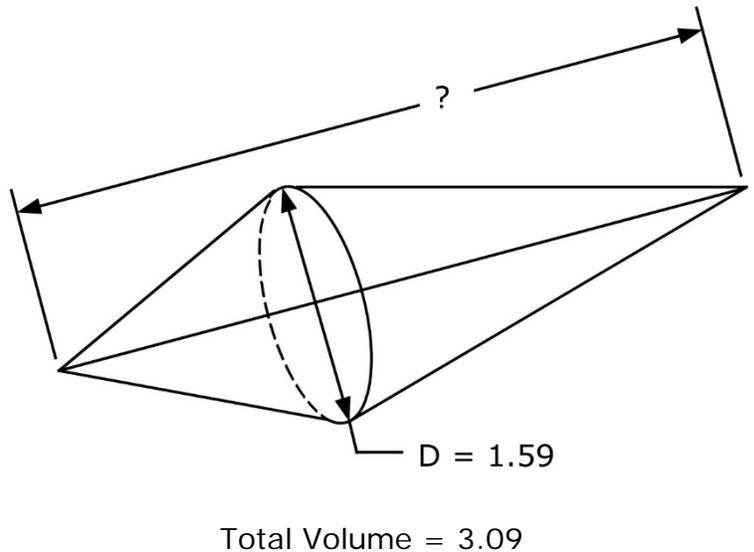


Cube Volume = Cylinder Volume

20B-49 = _____

20B-50.

CONES



20B-50 = _____

20B-51. $10^{+(0.759)} + 10^{-(0.171)} + [10^{(0.514/0.326)} - 10^{(1.57)}]^{1/2}$ -- 51=_____

20B-52. $\frac{1 + e^{\{0.825 + (0.371)(1.93)\}}}{(-6.73 \times 10^{-4})(\pi - e^{(-0.199)})}$ ----- 52=_____

20B-53. $\frac{(0.508) \text{Log}(-0.548 + 2.97)}{\text{Log}(0.779) - (0.961)(0.36)}$ ----- 53=_____

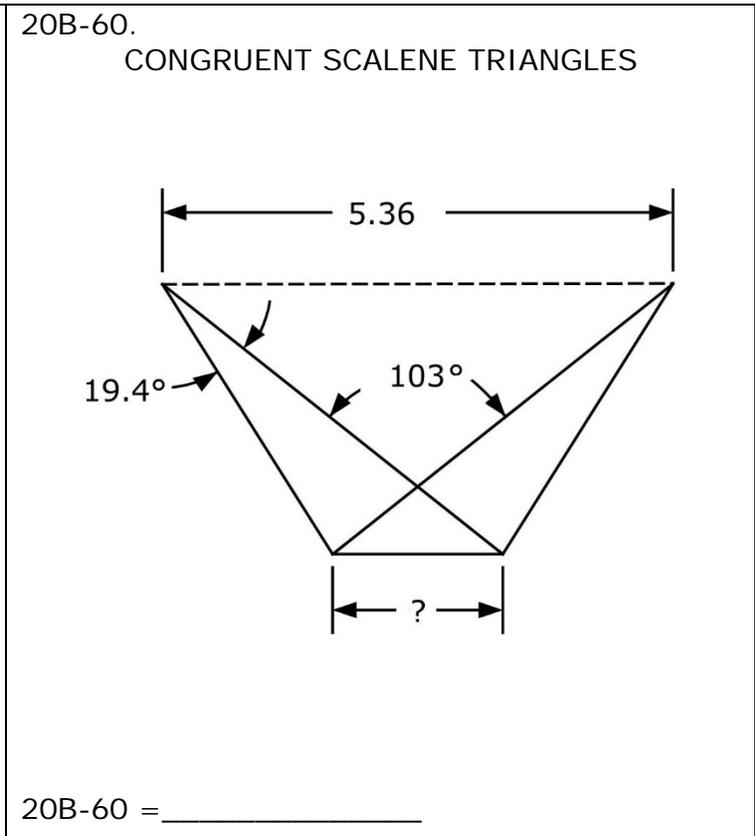
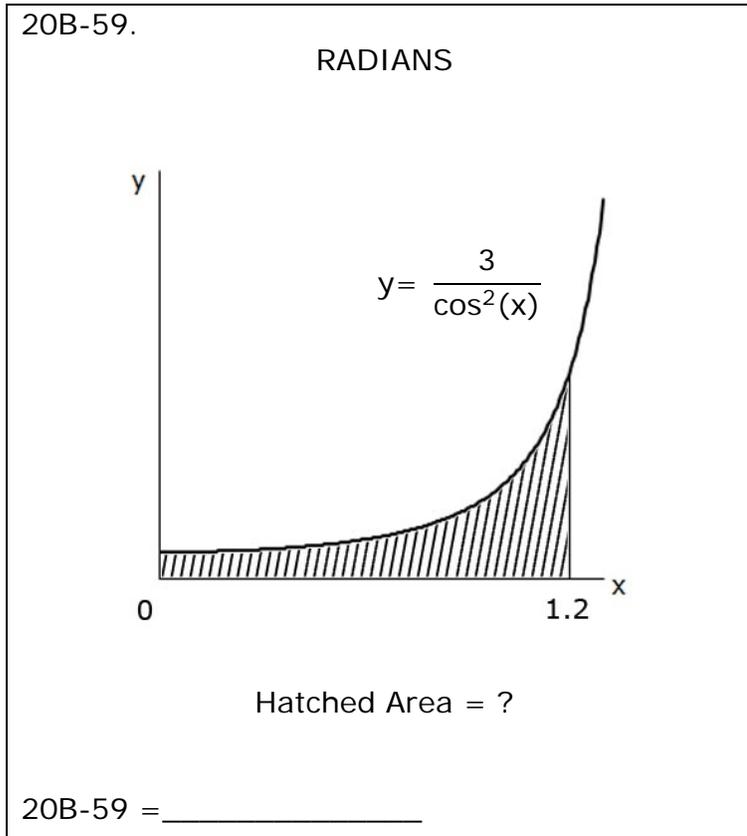
20B-54. $\frac{(-31.8 + 66.2)^{-0.577}}{(15.1)^{-(0.685 + 0.749)}}$ ----- 54=_____

20B-55. (rad) $\frac{\arctan\{7.3 + (7.93)(0.645)\}}{\arcsin\{(78.7 + 54.5)/1210\}}$ ----- 55=_____

20B-56. (rad) Calculate the slope of the curve $y = x^2 \cos(x)$ at $x = 13$. ----- 56=_____

20B-57. A sector has a perimeter of 10 in. What is R if the area is maximized? ----- 57=_____ in

20B-58. Solve for K_{22} if $\mathbf{K} = 2\mathbf{L} + 5\mathbf{M}$, $\mathbf{L} = \begin{bmatrix} 41 & 48 \\ 48 & 43 \end{bmatrix}$, and $\mathbf{M} = \begin{bmatrix} -12 & 16 \\ 16 & 9 \end{bmatrix}$.---- 58=_____

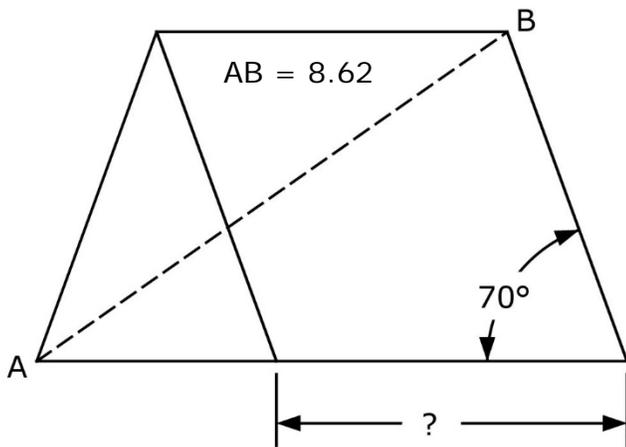


20B-61. Sailing around the world requires traveling a distance greater than the earth's circumference due to the land masses. A yacht sails at 7 knots and takes 2 years to sail around the world, sailing 8 hr/dy. If a knot is 1.151 mph, how much further does the yacht travel than the earth circumference? ----- 61 = _____ mi

20B-62. Solve 5^{5^5} . ----- 62 = _____

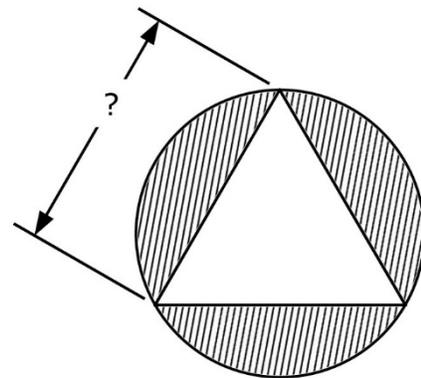
20B-63. A soldier fires a charge at an angle of 35° relative to horizontal at a target that is on the ground 1 mi off. They miss their target by 138 ft, landing short. What should the new angle be to hit the target? ----- 63 = _____ $^\circ$

20B-64. ISOSCELES TRIANGLE AND RHOMBUS



20B-64 = _____

20B-65. EQUILATERAL TRIANGLE AND CIRCLE



Hatched Area = 110

20B-65 = _____

20B-66. $\text{Log}(6.49) + \text{Log}(1.64) + \text{Log}(6.65) + \text{Log} \left[\frac{(4.34)}{(1.64)} \right]$ ----- 66 = _____

20B-67. $e^{\text{Ln}[(9.52)(90.6)]} + 10^{\text{Log}[(0.754)(660)]}$ ----- 67 = _____

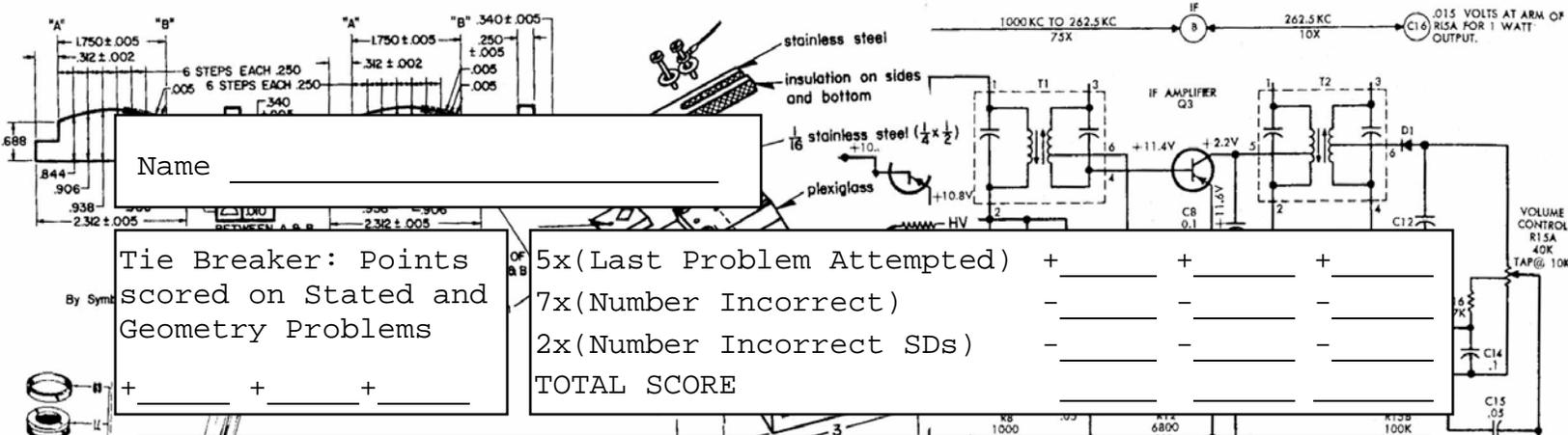
20B-68. $(\text{deg}) \sin(-13.4^\circ)\cos(109^\circ) + \cos(-13.4^\circ)\sin(109^\circ)$ ----- 68 = _____

20B-69. $1 + \frac{(0.85)^4}{2} - \frac{(0.85)^6}{6} + \frac{(0.85)^8}{24} - \frac{(0.85)^{10}}{120}$ ----- 69 = _____

20B-70. $\frac{1}{\sqrt{(69.7)^2 - (2260)}} \text{Ln} \left\{ \frac{(140) - \sqrt{(69.7)^2 - (2260)}}{(140) + \sqrt{(69.7)^2 - (2260)}} \right\}$ ----- 70 = _____

20B-1	= 1.15 = 1.15×10^0	20B-11	= -480000 = -4.80×10^5	20B-21	= -0.246 = -2.46×10^{-1}
20B-2	= -17.4 = -1.74×10^1	20B-12	= 4.65×10^{-8}	20B-22	= 0.428 = 4.28×10^{-1}
20B-3	= -0.0784 = -7.84×10^{-2}	20B-13	= 2.14×10^7	20B-23	= 1.06×10^8
20B-4	= 174 = 1.74×10^2	20B-14	= 0.513 = 5.13×10^{-1}	20B-24	= 5.55 = 5.55×10^0
20B-5	= 0.000254 = 2.54×10^{-4}	20B-15	= 0.00305 = 3.05×10^{-3}	20B-25	= 0.281 = 2.81×10^{-1}
20B-6	= 6.08 = 6.08×10^0	20B-16	= \$67,237.16	20B-26	= 0.288 = 2.88×10^{-1}
20B-7	= 31500 = 3.15×10^4	20B-17	= -4.51 = -4.51×10^0	20B-27	= 3 integer
20B-8	= 1.62 = 1.62×10^0	20B-18	= 4.40 = 4.40×10^0	20B-28	= 16.349 = 1.6349×10^1 (5SD)
20B-9	= 142 = 1.42×10^2	20B-19	= 1.23 = 1.23×10^0	20B-29	= 0.359 = 3.59×10^{-1}
20B-10	= 0.00215 = 2.15×10^{-3}	20B-20	= 15.1 = 1.51×10^1	20B-30	= 17.7 = 1.77×10^1

20B-31	= -66.7 = -6.67×10^1	20B-41	= 3.45 = 3.45×10^0	20B-51	= 7.17 = 7.17×10^0	20B-61	= 22200 = 2.22×10^4
20B-32	= 3190 = 3.19×10^3	20B-42	= -0.464 = -4.64×10^{-1}	20B-52	= -3630 = -3.63×10^3	20B-62	= 1.91×10^{2184}
20B-33	= 0.00200 = 2.00×10^{-3}	20B-43	= -0.222 = -2.22×10^{-1}	20B-53	= -0.429 = -4.29×10^{-1}	20B-63	= 37.4 = 3.74×10^1
20B-34	= 2.62 = 2.62×10^0	20B-44	= 3.02×10^{-6}	20B-54	= 6.37 = 6.37×10^0	20B-64	= 5.26 = 5.26×10^0
20B-35	= 32.6 = 3.26×10^1	20B-45	= -0.944 = -9.44×10^{-1}	20B-55	= 13.5 = 1.35×10^1	20B-65	= 13.4 = 1.34×10^1
20B-36	= 270 = 2.70×10^2	20B-46	= 2050 = 2.05×10^3	20B-56	= -47.4 = -4.74×10^1	20B-66	= 2.27 = 2.27×10^0
20B-37	= 19.3 = 1.93×10^1	20B-47	= 18.9 = 1.89×10^1	20B-57	= 2.50 = 2.50×10^0	20B-67	= 1360 = 1.36×10^3
20B-38	= 7.68 = 7.68×10^0	20B-48	= 4.34 = 4.34×10^0	20B-58	= 131 = 1.31×10^2	20B-68	= 0.995 = 9.95×10^{-1}
20B-39	= 3.02 = 3.02×10^0	20B-49	= 70.5 = 7.05×10^1	20B-59	= 7.72 = 7.72×10^0	20B-69	= 1.21 = 1.21×10^0
20B-40	= 77.0 = 7.70×10^1	20B-50	= 4.67 = 4.67×10^0	20B-60	= 1.79 = 1.79×10^0	20B-70	= -0.0150 = -1.50×10^{-2}



Name _____

Tie Breaker: Points scored on Stated and Geometry Problems
 + _____ + _____ + _____

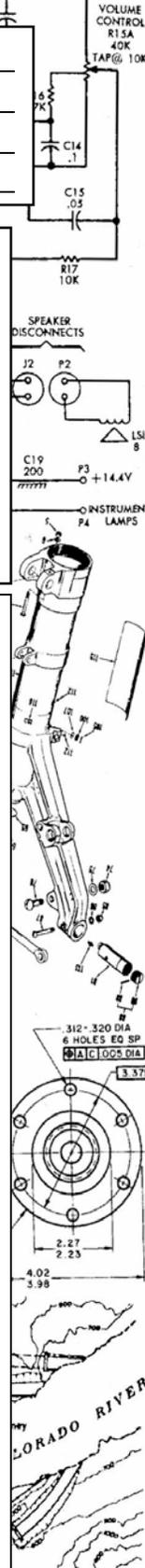
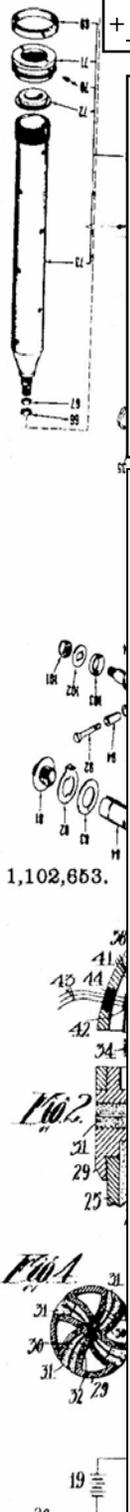
5x(Last Problem Attempted) + _____ + _____ + _____
 7x(Number Incorrect) - _____ - _____ - _____
 2x(Number Incorrect SDs) - _____ - _____ - _____
 TOTAL SCORE _____

UIL Calculator Applications

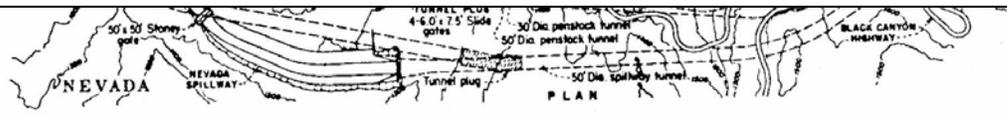
Test 20F (District)

DO NOT OPEN THE TEST UNTIL INSTRUCTED TO BEGIN

- I. Calculator Applications rules and scoring—See UIL Constitution
 - II. How to write the answers
 - A. For all problems except stated problems as noted below—write three significant digits.
 - 1. Examples (* means correct but not recommended)
 - Correct: 12.3, 123, 123.*, 1.23x10*, 1.23x10^{0*}
 1.23x10¹, 1.23x10⁰¹, .0190, 0.0190, 1.90x10⁻²
 - Incorrect: 12.30, 123.0, 1.23(10)², 1.23•10², 1.230x10²,
 1.23*10², 0.19, 1.9x10⁻², 19.0x10⁻³, 1.90E-02
 - 2. Plus or minus one digit error in the third significant digit is permitted.
 - B. For stated problems
 - 1. Except for integer, dollar sign, and significant digit problems, as detailed below, answers to stated problems should be written with three significant digits.
 - 2. Integer problems are indicated by (integer) in the answer blank. Integer problems answers must be exact, no plus or minus one digit, no decimal point or scientific notation.
 - 3. Dollar sign (\$) problems should be answered to the exact cent, but plus or minus one cent error is permitted. Answers must be in fixed notation. The decimal point and cents are required for exact-dollar answers.
 - 4. Significant digit problems are indicated by underlined numbers and by (SD) in the answer blank. See the UIL Constitution and Contest Manual for details.
- III. Some symbols used on the test
 - A. Angle measure: rad means radians; deg means degrees.
 - B. Inverse trigonometric functions: arcsin for inverse sine, etc.
 - C. Special numbers: π for 3.14159 ...; e for 2.71828 ...
 - D. Logarithms: Log means common (base 10); Ln means natural (base e); exp(u) means e^u.



Witnesses:
 G. P. Wilson
 S. J. Hartnett



20F-1. $(-9.11 - 7.73)/(7.88)$ ----- 1= _____

20F-2. $(48 + 9.32 - 2.22) \times 47.6$ ----- 2= _____

20F-3. $(-1.28 - 0.702 + 1.87 + 0.558)/(-7.77)$ ----- 3= _____

20F-4. $\{(42.9 - 35.1 + 114)(-8.79)(9.26)\} - 3790$ ----- 4= _____

20F-5. $\frac{12100 + 9390}{(837)(283)(-65.5)} + 0.00205 - 4.09 \times 10^{-4}$ ----- 5= _____

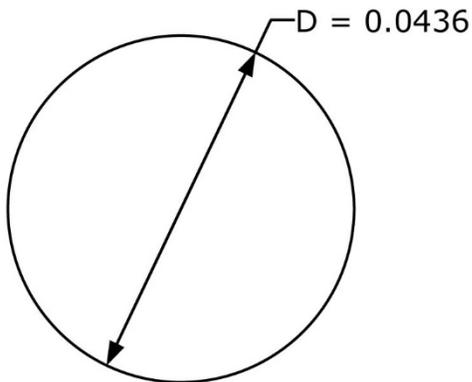
20F-6. What is the average of 5.98, 3.22 and π ? ----- 6= _____

20F-7. What is the positive product of the square root of 44.4 and the cube root of 999? ----- 7= _____

20F-8. What is the positive square root of the sum of 29.6 and π^2 ? ----- 8= _____

20F-9.

CIRCLE

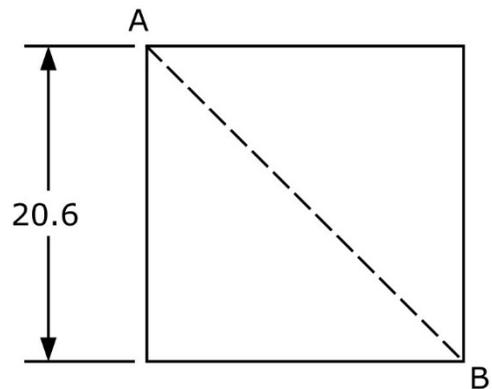


Area = ?

20F-9 = _____

20F-10.

SQUARE



AB = ?

20F-10 = _____

20F-11. $\frac{(-0.00826)(0.0128) - (-0.0027)(0.032) + 8.74 \times 10^{-5}}{-0.00211 + (0.0306)(-0.0635)}$ ----- 11 = _____

20F-12. $\frac{(-0.378 + 0.039 - 0.0599)(-0.502)(-0.397)}{(1.99 - 1.31)(-0.656 - 1.89)}$ ----- 12 = _____

20F-13. $\frac{6.10 \times 10^5 + 2.00 \times 10^6}{(-0.904)(-0.939) + 2.23} + \frac{7620 - 5650 + 6360}{(5.02 \times 10^{-4})(17.2)}$ ----- 13 = _____

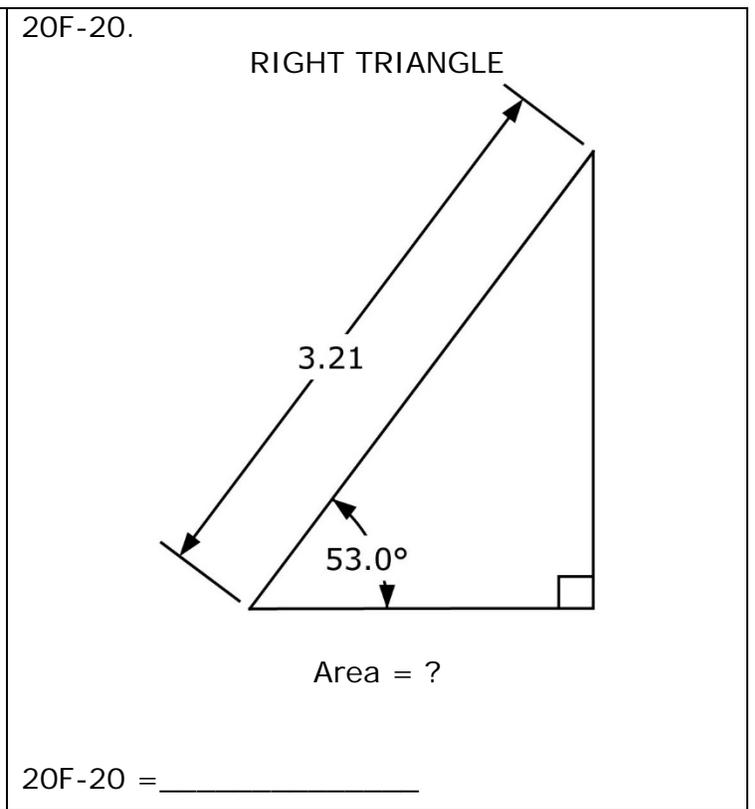
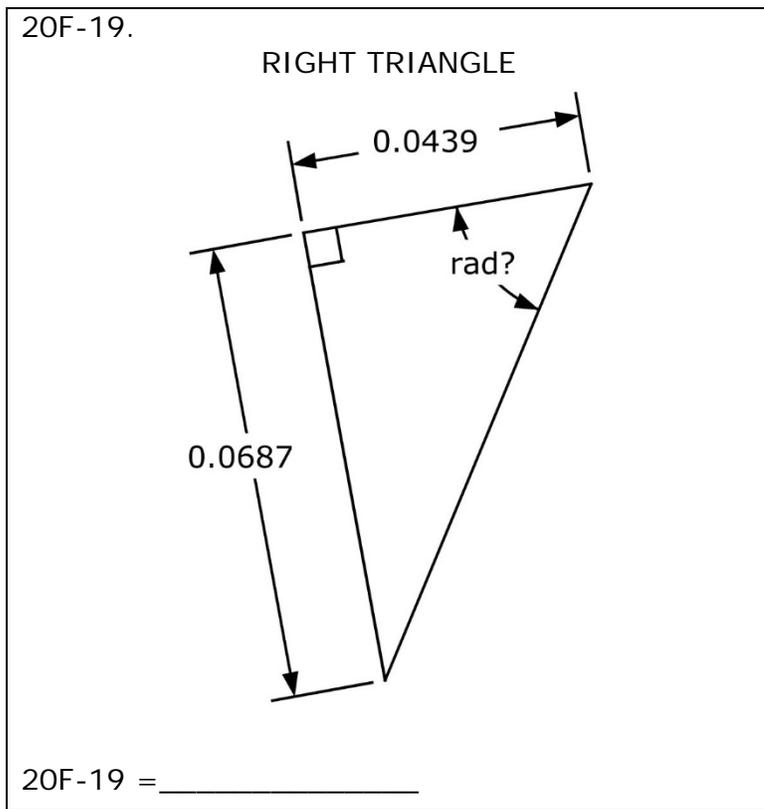
20F-14. $\frac{875 + 239 - 319}{(0.419)(59.4)} - \frac{(14900)(8.84 \times 10^{-4} + 2.82 \times 10^{-4})}{0.637 + 0.165 - 0.177}$ ----- 14 = _____

20F-15. $\frac{(98400 + 22200 - 71300)(0.447 - 0.33 - 0.479)}{(598)(829)(-32.9)(3.72 + 1.28 + \pi)}$ ----- 15 = _____

20F-16. Rock Springs, Texas is 58.5 mi from Rocksprings, Texas. How long does it take to drive this distance at 55 mph? ----- 16 = _____ min

20F-17. For a fundraiser, Don buys 12 extra large pizzas and then resales slices for \$2 each at a park. There are 10 slices per pizza, and he pays \$13 for each pizza. What is his profit, if there are 7 slices left over? ----- = \$ _____

20F-18. A Fibonacci series is extended by adding the previous two numbers in the series. The first six Fibonacci numbers are 0, 1, 1, 2, 3, 5. What is the tenth Fibonacci number? ----- 18 = _____ integer



20F-21. $\sqrt{\frac{(7.46)(2.63)}{331 + 109}} + 0.151$ ----- 21= _____

20F-22. $\frac{1}{0.237 + 0.661} + \frac{1}{0.118 - 0.251} + \frac{1}{(0.759)}$ ----- 22= _____

20F-23. $[-83.2 + \sqrt{6200}]^2 \times [891 + 6600]^2 \times \sqrt{0.358/0.893}$ ----- 23= _____

20F-24. $\left[\frac{1.24 + 0.582 + \sqrt{0.543/0.411}}{0.0907 + 0.0181} \right]^2$ ----- 24= _____

20F-25. $\frac{\sqrt{8.7 + 6.84 + (75.4)/(9.52)}}{5.19 + 4.53}$ ----- 25= _____

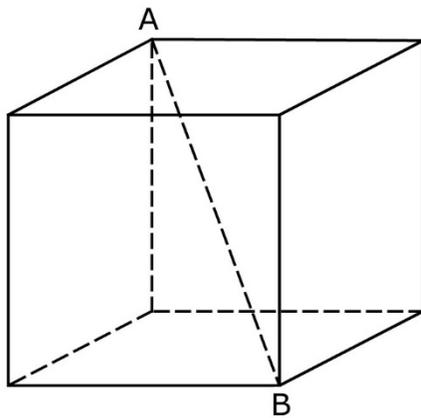
20F-26. The return stroke of current that causes the visible flash of lightning travels at a speed of about 320 million ft/s. What fraction of the speed of light is this, if the speed of light is 186,000 mi/s? ----- 26= _____ %

20F-27. A football field is 160 ft wide. What is the area of the football field between the 5-yard lines? ----- 27= _____ acres

20F-28. A church band plays 7 songs every week, 3 of which are new, having never been played before. On average, what is the fewest number of different songs played by the band in a year? ----- 28= _____

20F-29.

CUBE



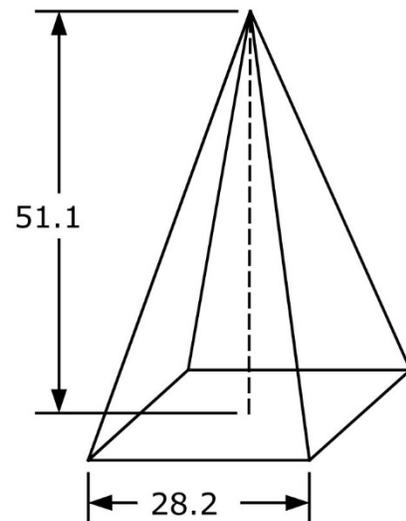
AB = 263

Surface Area = ?

20F-29 = _____

20F-30.

SQUARE PYRAMID



Volume = ?

20F-30 = _____

20F-31. $\frac{(-4.26 \times 10^{-7} + 8.71 \times 10^{-7})^2}{\sqrt{47.9 - 26.8}} + \frac{4.60 \times 10^{-17}}{\sqrt{8.08 \times 10^{-7} + 1.17 \times 10^{-6}}}$ ----- 31 = _____

20F-32. $\sqrt{\frac{1/(973 - 169)}{(270)(1.36 + 0.925)^2}} + (6.81 \times 10^{-7})^2(2.76 \times 10^9)$ ----- 32 = _____

20F-33. $\frac{[(525 - 260)(0.638/0.648)]^{1/2}}{(0.58)^2 + (0.243 + 0.374)^2 + 0.211}$ ----- 33 = _____

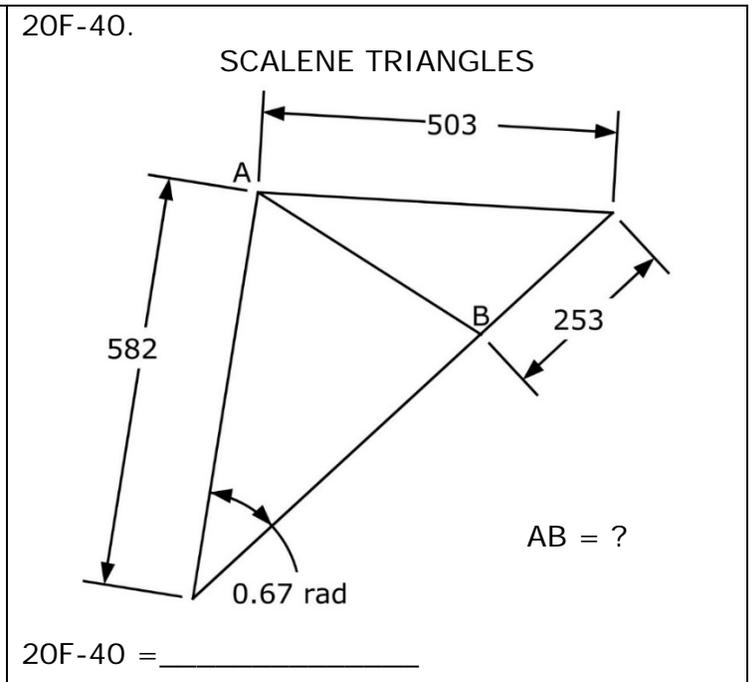
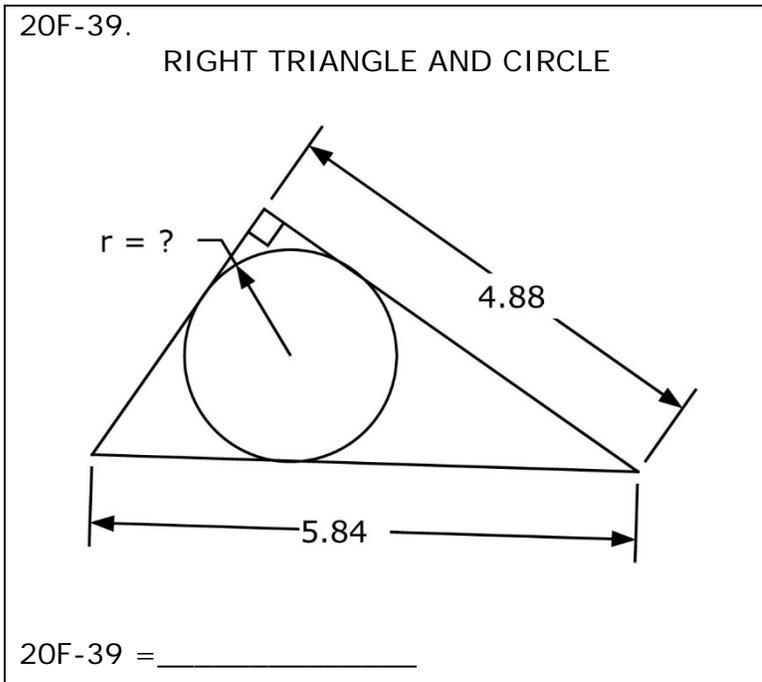
20F-34. $\frac{[4790/(0.801 + 0.467) + 1/(1.32 \times 10^{-4})]^{1/2}}{(4.03 \times 10^{-4} + 5.81 \times 10^{-4})^2 \times \sqrt{7.62 \times 10^{-4} - (-6.32 \times 10^{-4})}}$ ----- 34 = _____

20F-35. $\frac{\left[\frac{(-67500 + 40600)}{(984 + 1380)}\right]^2 + \sqrt{\frac{10300 + 14200}{\sqrt{0.171}}}}{\{(-52900)/(46300)\}^2}$ ----- 35 = _____

20F-36. The perimeter of a square plot was estimated to be 355.5 ft. A surveyor measured one side to be 89 ft 1.3 in. What is the percent error in the estimate? ----- 36 = _____ % (SD)

20F-37. In a locale, a bug population doubles every 25 days. The birds eat the bugs. There's 1800 birds that each eat 28 bugs a day. If an equilibrium bug population is reached, how many bugs are in the locale? Base your answer on the increase in bugs in 1 hour. ----- 37 = _____

20F-38. A mercury fever thermometer has a bulb of mercury that expands as it is heated, moving it into a thin capillary tube that is scaled to measure the temperature. The bulb is cylindrical, 0.5 in long with a diameter of 0.16 in. The mercury volume increases by 10^{-4} for every degree (F) change. If a 1°F change in temperature moves the thermometer reading 0.2 in, what is the capillary diameter? ----- 38 = _____ milli-in



20F-41. $(0.00402)(0.00954)10^{\{0.00995/0.00533\}}$ ----- 41 = _____

20F-42. $\frac{e^{+0.9} + e^{-0.866}}{(0.00971 + 0.0054)}$ ----- 42 = _____

20F-43. $(-0.00271 - 0.00324) \ln\{(-0.00353)(-3.89 \times 10^{-4})\}$ ----- 43 = _____

20F-44. $(7.18)^3 + (38.1 - 7.54)^{1.54}$ ----- 44 = _____

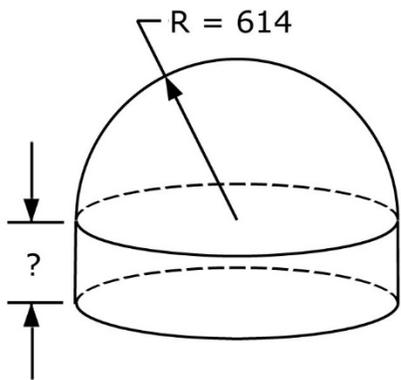
20F-45. $(\text{deg}) \{(6.69 \times 10^{-6}) \sin(-151^\circ)\} \times \{(-4.69 \times 10^{-6}) \cos(-29.9^\circ)\}$ --- 45 = _____

20F-46. An 8-in tall model of a 3D artwork required 2 oz of paint to complete it. How much paint will be needed for the 12-ft tall actual artwork? ----- 46 = _____ gal

20F-47. The density of water (g/cc) is temperature dependent. From 10°C to 50°C in 10-degree increments, the density is: 0.999728, 0.998234, 0.995678, 0.992247, 0.988066. What is the percent error in the extrapolated density at 90°C and the actual value, 0.965340? ----- 47 = _____ %(SD)

20F-48. Solve for h if $h = \frac{6}{h} - \sqrt{h}$. ----- 48 = _____

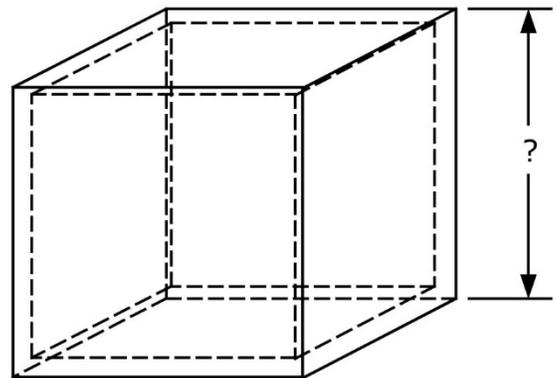
20F-49. CYLINDER AND HEMISPHERE



Cylinder Total Surface Area = Hemisphere Total Surface Area

20F-49 = _____

20F-50. HOLLOW CUBE WITH WALL THICKNESS t



t = 0.679
Hollow Cube Volume = 349,000

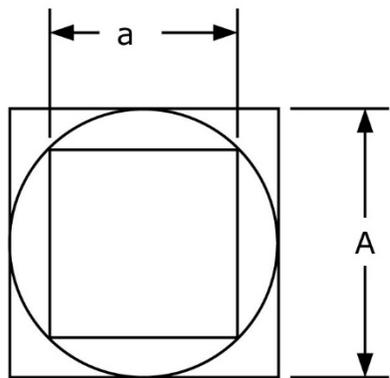
20F-50 = _____

20F-61. Summers in Texas are hot. The high temperature is 100°F at 5 PM and the low is 75°F at 5 AM. Assuming a sinusoidal temperature variation, what is the temperature at 1 PM? ----- 61= _____ °F

20F-62. The probability of being dealt "four of a kind" in poker is 1 in 4165. What is the probability of being dealt four of a kind 160 times in a row? ----- 62= _____

20F-63. An object is thrown off the roof of a 285-ft tall building with a release angle of 33° relative to the horizontal. The release velocity was 37 mph. What is the time of flight of the object? ----- 63= _____ s

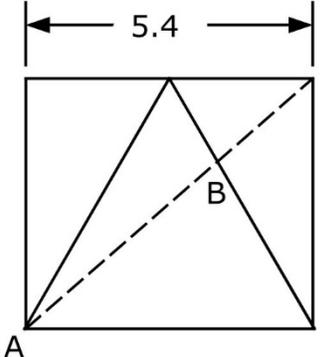
20F-64. SQUARES AND CIRCLE



$\frac{A}{a} = ?$

20F-64 = _____

20F-65. EQUILATERAL TRIANGLE AND RECTANGLE



$AB = ?$

20F-65 = _____

20F-66. $\text{Ln} \left[\frac{(3.39)^2 - 2(3.39)(11.6) + (11.6)^2}{(117)^2} \right]^2$ ----- 66= _____

20F-67. (rad) $\cos(0.56 - 0.27) - \cos(0.56 + 0.27)$ ----- 67= _____

20F-68. (deg) $\sqrt{1 + \left[\frac{\cos(76.5^\circ)}{\sin(76.5^\circ)} \right]^2} \times \frac{\cos(-31.1^\circ)}{\sin(-31.1^\circ)}$ ----- 68= _____

20F-69. $\frac{1}{(0.14)} + \frac{1}{3(0.14)^3} + \frac{1}{5(0.14)^5} + \frac{1}{7(0.14)^7}$ ----- 69= _____

20F-70. (rad) $e^{(7.89)} \left[\frac{(0.265)\sin(2) - (0.18)\cos(-0.438)}{(9.76)\sqrt{(0.265)^2 + (0.18)^2}} \right]$ ----- 70= _____

20F-1	= -2.14 = -2.14×10^0	20F-11	= -0.0168 = -1.68×10^{-2}	20F-21	= 0.362 = 3.62×10^{-1}
20F-2	= 2620 = 2.62×10^3	20F-12	= 0.0459 = 4.59×10^{-2}	20F-22	= -5.09 = -5.09×10^0
20F-3	= -0.0574 = -5.74×10^{-2}	20F-13	= 1.81×10^6	20F-23	= 7.07×10^8
20F-4	= -13700 = -1.37×10^4	20F-14	= 4.14 = 4.14×10^0	20F-24	= 746 = 7.46×10^2
20F-5	= 0.000256 = 2.56×10^{-4}	20F-15	= 0.000134 = 1.34×10^{-4}	20F-25	= 0.498 = 4.98×10^{-1}
20F-6	= 4.11 = 4.11×10^0	20F-16	= 63.8 = 6.38×10^1	20F-26	= 32.6 = 3.26×10^1
20F-7	= 66.6 = 6.66×10^1	20F-17	= \$70.00	20F-27	= 0.992 = 9.92×10^{-1}
20F-8	= 6.28 = 6.28×10^0	20F-18	= 34 integer	20F-28	= 161 = 1.61×10^2
20F-9	= 0.00149 = 1.49×10^{-3}	20F-19	= 1.00 = 1.00×10^0	20F-29	= 138,000 = 1.38×10^5
20F-10	= 29.1 = 2.91×10^1	20F-20	= 2.48 = 2.48×10^0	20F-30	= 13500 = 1.35×10^4

20F-31	= 7.58x10 ⁻¹⁴ = 0.00282 = 2.82x10 ⁻³	20F-41	= 0.00282 = 2.82x10 ⁻³	20F-51	= 0.0939 = 9.39x10 ⁻²	20F-61	= 93.8 = 9.38x10 ¹
20F-32	= 0.00222 = 2.22x10 ⁻³	20F-42	= 191 = 1.91x10 ²	20F-52	= -0.000282 = -2.82x10 ⁻⁴	20F-62	= 7.27x10 ⁻⁵⁸⁰
20F-33	= 17.4 = 1.74x10 ¹	20F-43	= 0.0803 = 8.03x10 ⁻²	20F-53	= 29.7 = 2.97x10 ¹	20F-63	= 5.23 = 5.23x10 ⁰
20F-34	= 2.95x10 ⁹	20F-44	= 564 = 5.64x10 ²	20F-54	= 1.77 = 1.77x10 ⁰	20F-64	= 1.41 = 1.41x10 ⁰
20F-35	= 286 = 2.86x10 ²	20F-45	= 1.32x10 ⁻¹¹	20F-55	= 10.3 = 1.03x10 ¹	20F-65	= 4.76 = 4.76x10 ⁰
20F-36	= -0.26 = -2.6x10 ⁻¹ (2SD)	20F-46	= 5.06 = 5.06x10 ⁰	20F-56	= 62.5 = 6.25x10 ¹	20F-66	= -10.6 = -1.06x10 ¹
20F-37	= 1.82x10 ⁶	20F-47	= 1.229 = 1.229x10 ⁰ (4SD)	20F-57	= 210 = 2.1x10 ²	20F-67	= 0.283 = 2.83x10 ⁻¹
20F-38	= 2.53 = 2.53x10 ⁰	20F-48	= 1.86 = 1.86x10 ⁰	20F-58	= 267 = 2.67x10 ²	20F-68	= -1.70 = -1.70x10 ⁰
20F-39	= 1.12 = 1.12x10 ⁰	20F-49	= 307 = 3.07x10 ²	20F-59	= 45.0 = 4.50x10 ¹	20F-69	= 139000 = 1.39x10 ⁵
20F-40	= 374 = 3.74x10 ²	20F-50	= 293 = 2.93x10 ²	20F-60	= 85.6 = 8.56x10 ¹	20F-70	= 66.6 = 6.66x10 ¹